

Introduction to Computer Security

Lecture 3

Take Grant Model (Cont) HRU Schematic Protection Model

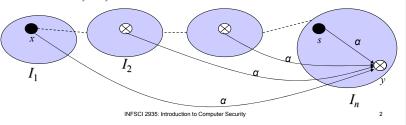
September 16, 2004

Courtesy of Professors Chris Clifton & Matt Bishop INFSCI 2935: Introduction of Computer Security

Theorem: Can_share($\alpha, \mathbf{x}, \mathbf{y}, G_0$) (for subjects)



- Subject_can_share(α, x, y,G₀) is true iff x and y are subjects and
 - there is an α edge from x to y in G_0 OR if:
 - \bigcirc ∃ a subject s ∈ G_0 with an s-to-y α edge, and
 - \bigcirc \exists islands I_1,\ldots,I_n such that ${\pmb x}\in I_1,$ ${\pmb s}\in I_n,$ and there is a bridge from I_i to I_{j+1}



What about objects? Initial, terminal spans



- x initially spans to y if x is a subject and there is a tg-path associated with word $\{t_{\rightarrow} * g_{\rightarrow}\}$ between them
 - $\bigcirc x$ can grant a right to y
- x terminally spans to y if x is a subject and there is a tg-path associated with word $\{t_{\rightarrow}^*\}$ between them
 - $\bigcirc x$ can take a right from y

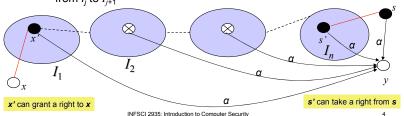
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Theorem: Can_share($\alpha, \mathbf{x}, \mathbf{y}, G_0$)



- Can_share(α, x, y, G_0) iff there is an α edge from x to y in G_0 or if:
 - $\bigcirc \exists$ a vertex $s \in G_0$ with an s to $y \alpha$ edge,
 - \bigcirc \exists a subject x' such that x'=x or x' initially spans to x,
 - \bigcirc \exists a subject s ' such that s '=s or s ' terminally spans to s, and
 - \bigcirc \exists islands $I_1, \, ..., \, I_n$ such that $x \, ' \in I_1, \, s \, ' \in I_n$, and there is a bridge from I_j to I_{j+1}







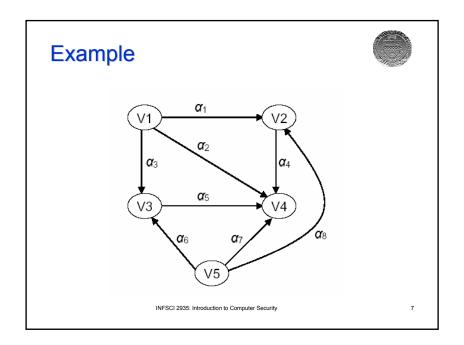
- Corollary: There is an O(|V|+|E|) algorithm to test can share: Decidable in linear time!!
- Theorem
 - \bigcirc Let G_0 contain exactly one vertex and no edges,
 - R a set of rights.
 - G₀ | * G iff G is a finite directed acyclic graph, with edges labeled from R, and at least one subject with no incoming edge.
 - Only if part: v is initial subject and $G_0 \vdash *G$;
 - No rule allows the deletion of a vertex
 - No rule allows an incoming edge to be added to a vertex without any incoming edges. Hence, as v has no incoming edges, it cannot be assigned any

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Theorem: Can_share($\alpha, \mathbf{x}, \mathbf{y}, G_0$)



- *If* part : *G* meets the requirement
 - Assume v is the vertex with no incoming edge and apply rules
 - 1. Perform "v creates ($\alpha \cup \{g\}$ to) new x_i " for all 2<=i <= n, and α is union of all labels on the incoming edges going into x_i in G
 - 2. For all pairs x, y with x α over y in G, perform "v grants (α to y) to x"
 - 3. If β is the set of rights x has over y in G, perform "v removes ($\alpha \cup \{g\} \beta$) to y"



Take-Grant Model: Sharing through a Trusted Entity



- Let p and q be two processes
- Let *b* be a buffer that they share to communicate
- Let s be third party (e.g. operating system) that controls b



Theft in Take-Grant Model



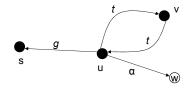
- Can_steal(α ,**x**,**y**, G_0) is true if there is no α edge from **x** to **y** in G_0 and \exists sequence G_1 , ..., G_n s. t.:
 - $\bigcirc \exists \alpha \text{ edge from } \mathbf{x} \text{ to } \mathbf{y} \text{ in } G_n$,
 - $\bigcirc \exists$ rules $\rho_1,..., \rho_n$ that take $G_{i-1} \vdash \rho_i G_i$, and
 - $\bigcirc \forall \mathbf{v}, \mathbf{w} \in G_i$, $1 \le i < n$, if $\exists \alpha$ edge from \mathbf{v} to \mathbf{y} in G_0 then ρ_i is not " \mathbf{v} grants (α to \mathbf{y}) to \mathbf{w} "
 - Disallows owners of $\boldsymbol{\alpha}$ rights to y from transferring those rights
 - Does not disallow them to transfer other rights
 - This models a Trojan horse

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A witness to theft



- u grants (t to v) to s
- s takes (t to u) from v
- s takes (α to w) from u



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Theorem: When Theft Possible



- Can_steal(α ,**x**,**y**, G_0) iff there is no α edge from **x** to **y** in G_0 and $\exists G_1, ..., G_n$ s. t.:
 - \bigcirc There is no α edge from **x** to **y** in G_0 ,
 - ∃ subject x' such that x'=x or x' initially spans to x, and
 - $\bigcirc \exists$ **s** with α edge to **y** in G_0 and can_share $(t, \mathbf{x}, \mathbf{s}, G_0)$
- Proof:
 - ⇒: Assume the three conditions hold
 - x can get t right over s (x is a subject) and then take α right over y from s
 - x' creates a surrogate to pass α to x (x is an object)
 - X' initially spans to x (Theorem 3.10 can_share(t,x',s,G₀))



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Theorem: When Theft Possible



- ←: Assume can_steal is true:
 - No α edge from definition 3.10 in G_0 .
 - Can_share(α ,**x**,**y**, G_0) from definition 3.10 condition (a): α from **x** to **y** in G_n
 - s exists from can_share and earlier theorem
 - Show Can_share($t, \mathbf{x}, \mathbf{s}, G_0$) holds: \mathbf{s} can't grant α (definition), someone else must get α from \mathbf{s} , show that this can only be accomplished with take rule

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Conspiracy



- Theft indicates cooperation: which subjects are actors in a transfer of rights, and which are not?
- Next question is
 - O How many subjects are needed to enable $Can_share(\alpha, x, y, G_0)$?
- Note that a vertex y
 - O Can take rights from any vertex to which it terminally spans
 - O Can pass rights to any vertex to which it initially spans
- Access set A(y) with focus y (y is subject) is union of
 - set of vertices y,
 - overtices to which y initially spans, and
 - overtices to which y terminally spans

Conspiracy



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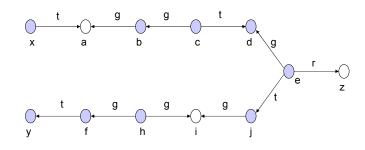
- Deletion set δ(y,y'): All z ∈ A(y) ∩ A(y') for which
 - y initially spans to z and y' terminally spans to z
 - y terminally spans to z and y' initially spans to z
 - ○z=y & z=y'
- Conspiracy graph H of G₀:
 - Represents the paths along which subjects can transfer rights
 - \bigcirc For each subject in G_0 , there is a corresponding vertex h(x) in H
 - \bigcirc if $\delta(y,y')$ not empty, edge from h(y) to h(y')

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Example





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Theorems



- I(p) =
 - contains the vertex h(p) and the se t of all vertices h(p') such that p' initially spans to p
- T(q) =
 - contains the vertex h(q) and the se t of all vertices h(q') such that q' terminally spans to q
- Theorem 3-13:
 - Can_share(α,x,y,G₀) iff there is a path from som h(p) in I(x) to some h(q) in T(y)
- Theorem 3-14:
 - O Let L be the number of vertices on a shortest path between h(p) and h(q) (as in theorem 3-13), then L conspirators are necessary and sufficient to produce a witness to Can share($\alpha, \mathbf{x}, \mathbf{y}, G_0$)

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Back to HRU: Fundamental questions



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- How can we determine that a system is secure?
 - Need to define what we mean by a system being "secure"
- Is there a generic algorithm that allows us to determine whether a computer system is secure?

Turing Machine & halting problem



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- The halting problem:
 - OGiven a description of an algorithm and a description of its initial arguments, determine whether the algorithm, when executed with these arguments, ever halts (the alternative is that it runs forever without halting).
- Reduce TM to Safety problem
 - Olf Safety problem is decidable then it implies that TM halts (for all inputs) – showing that the halting problem is decidable (contradiction)

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Turing Machine



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- TM is an abstract model of computer
 - Alan Turing in 1936
- TM consists of
 - OA tape divided into cells; infinite in one direction
 - A set of tape symbols *M*
 - M contains a special blank symbol b
 - A set of states *K*
 - O A head that can read and write symbols
 - OAn action table that tells the machine
 - What symbol to write
 - How to move the head ('L' for left and 'R' for right)
 - What is the next state

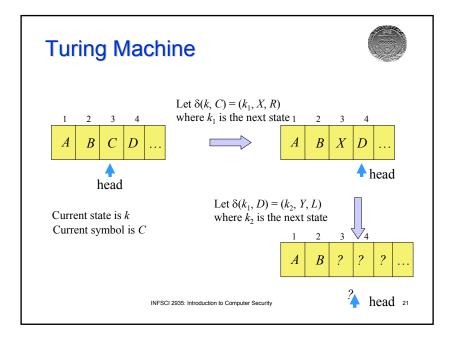
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Turing Machine



- The action table describes the transition function
- Transition function $\delta(k, m) = (k', m', L)$:
 - Oin state k, symbol m on tape location is replaced by symbol m',
 - Ohead moves to left one square, and TM enters state k'
- Halting state is q_f
 - OTM halts when it enters this state

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General Safety Problem



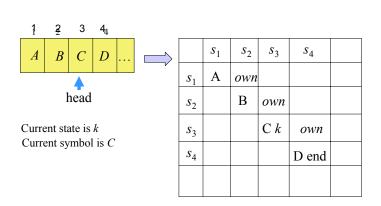
- Theorem: It is undecidable if a given state of a given protection system is safe for a given generic right
- Proof: Reduce TM to safety problem
 - \bigcirc Symbols, States \Rightarrow rights
 - ○Tape cell ⇒ subject
 - \bigcirc Cell s_i has $A \Rightarrow s_i$ has A rights on itself
 - \bigcirc Cell $s_k \Rightarrow s_k$ has end rights on itself
 - OState p, head at $s_i \Rightarrow s_i$ has p rights on itself
 - Objectinguished Right own:
 - $\circ s_i$ owns s_i+1 for $1 \le i < k$

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Mapping



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Command Mapping (Left move)



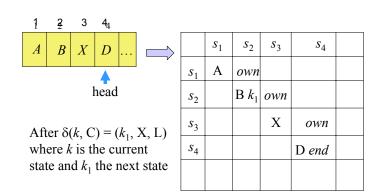
```
\delta(k, C) = (k_1, X, L)
\operatorname{command} c_{k,C}(s_i, s_{i-1})
\operatorname{if} own \ \operatorname{in} \ a[s_{i-1}, s_i] \ \operatorname{and} \ k \ \operatorname{in} \ a[s_i, s_i] \ \operatorname{and} \ C \ \operatorname{in} \ a[s_i, s_i]
\operatorname{delete} \ k \ \operatorname{from} \ A[s_i, s_i];
\operatorname{delete} \ C \ \operatorname{from} \ A[s_i, s_i];
\operatorname{enter} \ X \ \operatorname{into} \ A[s_i, s_i];
\operatorname{enter} \ k_1 \ \operatorname{into} \ A[s_{i-1}, s_{i-1}];
\operatorname{end}
```

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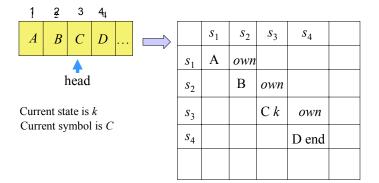
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Mapping (Initial)





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Command Mapping (Right move)



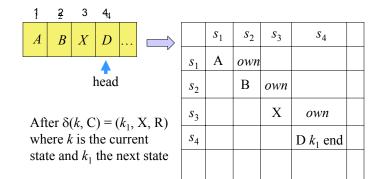
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```
\delta(k,\,\mathbf{C}) = (k_1,\,\mathbf{X},\,\mathbf{R})
\mathbf{command}\,\,\mathbf{c}_{k,\mathbf{C}}(s_i,\,s_{i+1})
\mathbf{if}\,\,own\,\,\mathbf{in}\,\,a[s_i,\,s_{i+1}]\,\,\mathbf{and}\,\,k\,\,\mathbf{in}\,\,a[s_i,\,s_i]\,\,\mathbf{and}\,\,\mathbf{C}\,\,\mathbf{in}\,\,a[s_i,\,s_i]
\mathbf{delete}\,\,k\,\,\mathbf{from}\,\,A[s_i,s_i];
\mathbf{delete}\,\,\mathbf{C}\,\,\mathbf{from}\,\,A[s_i,s_i];
\mathbf{enter}\,\,\mathbf{X}\,\,\mathbf{into}\,\,A[s_i,s_i];
\mathbf{enter}\,\,k_1\,\,\mathbf{into}\,\,A[s_{i+1},\,s_{i+1}];
\mathbf{end}
```

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Mapping





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Command Mapping (Rightmost move)

end



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```
\delta(k_1, D) = (k_2, Y, R) at end becomes
command crightmost<sub>k,C</sub>(s_i,s_{i+1}) if end in a[s_i,s_i] and k_1 in a[s_i,s_i] and D in a[s_i,s_i]</sub>
then
       delete end from a[s_i,s_i];

create subject s_{i+1};

enter own into a[s_i,s_{i+1}];

enter end into a[s_{i+1}, s_{i+1}];

delete k_1 from a[s_i,s_i];

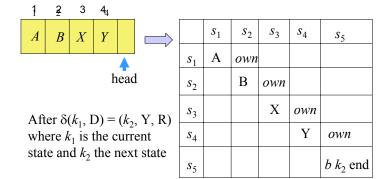
delete D from a[s_i,s_i];

enter Y into a[s_i,s_i];
```

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Mapping





Rest of Proof



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- Protection system exactly simulates a TM
 - Exactly 1 end right in ACM
 - 1 right corresponds to a state
 - Thus, at most 1 applicable command in each configuration of the TM
- If TM enters state q_f, then right has leaked
- If safety question decidable, then represent TM as above and determine if q_t leaks
 - ○Leaks halting state ⇒ halting state in the matrix ⇒ Halting state reached
- Conclusion: safety question undecidable

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Other theorems



- Set of unsafe systems is recursively enumerable
 - Recursively enumerable?
- For protection system without the create primitives, (i.e., delete create primitive); the safety question is complete in P-SPACE
- It is undecidable whether a given configuration of a given monotonic protection system is safe for a given generic right
 - Delete destroy, delete primitives;
 - The system becomes monotonic as they only increase in size and complexity

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Other theorems



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- The safety question for biconditional monotonic protection systems is undecidable
- The safety question for monoconditional, monotonic protection systems is decidable
- The safety question for monoconditional protection systems with create, enter, delete (and no destroy) is decidable.
- Observations
 - Safety is undecidable for the generic case
 - Safety becomes decidable when restrictions are applied

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Schematic Protection Model



- Key idea is to use the notion of a protection type
 - O Label that determines how control rights affect an entity
 - Take-Grant:
 - subject and object are different protection types
 - OTS and TO represent subject type set and object set
 - \circ $\tau(X)$ is the type of entity X
- A ticket describes a right
 - O Consists of an entity name and a right symbol: X/z
 - Possessor of the ticket X/z has right r over entity X
 - Y has tickets X/r, X/w -> Y has tickets X/rw
 - Each entity X has a set dom(X) of tickets Y/z
 - \circ $\tau(X/r:c) = \tau(X)/r:c$ is the type of a ticket

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Schematic Protection Model



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- Inert right vs. Control right
 - Olnert right doesn't affect protection state, e.g. read right
 - otake right in Take-Grant model is a control right
- Copy flag c
 - Every right r has an associated copyable right rc
 - *r:c* means *r* or *rc*
- Manipulation of rights
 - A link predicate
 - Determines if a source and target of a transfer are "connected"
 - A filter function
 - Determines if a transfer is authorized

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Transferring Rights



- dom(X): set of tickets that X has
- Link predicate: link_i(X,Y)
 - oconjunction or disjunction of the following terms
 - $X/z \in dom(X)$; $X/z \in dom(Y)$;
 - \bullet $\mathbf{Y}/z \in dom(\mathbf{X}); \mathbf{Y}/z \in dom(\mathbf{Y})$
 - true
 - O Determines if **X** and **Y** "connected" to transfer right
 - Examples:
 - Take-Grant: $link(X, Y) = Y/g \in dom(X) \vee X/t \in dom(Y)$
 - Broadcast: $link(X, Y) = X/b \in dom(X)$ • Pull: $link(X, Y) = Y/p \in dom(Y)$
 - Universal: link(X, Y) = true
- Scheme: a finite set of link predicates is called a scheme

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Filter Function



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- Filter function:
 - O Imposes conditions on when tickets can be transferred
 - f_i : $TS \times TS \rightarrow 2^{T \times R}$ (range is copyable rights)
- X/r:c can be copied from dom(Y) to dom(Z) iff ∃i s. t. the following are true:
 - \bigcirc X/rc \in dom(Y)
 - link_i(**Y**, **Z**)
 - \circ $\tau(X)/r:c \in f(\tau(Y), \tau(Z))$
- Examples:
 - \bigcirc If $f_i(\tau(\mathbf{Y}), \tau(\mathbf{Z})) = T \times R$ then any rights are transferable
 - Olf $f_i(\tau(\mathbf{Y}), \tau(\mathbf{Z})) = T \times RI$ then only inert rights are transferable
 - \bigcirc If $f_i(\tau(\mathbf{Y}), \tau(\mathbf{Z})) = \Theta$ then no tickets are transferable
- One filter function is defined for each link predicate

SCM Example 1



- Owner-based policy
 - Subject U can authorize subject V to access an object F iff U owns F
 - Types: TS= {user}, TO = {file}
 - Ownership is viewed as copy attributes
 - If U owns F, all its tickets for F are copyable
 - RI: { *r:c*, *w:c*, *a:c*, *x:c* }; RC is empty
 - read, write, append, execute; copy on each
 - $\bigcirc \ \forall \ U, \ V \in \text{user}, \ \textit{link}(U, \ V) = true$
 - Anyone can grant a right to anyone else if they posses the right to do so (copy)
 - \bigcirc f(user, user) = { file/r, file/w, file/a, file/x }
 - Can copy read, write, append, execute

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SPM Example 1



- Peter owns file Doom; can he give Paul execute permission over Doom?
 - $1.\tau(Peter)$ is user and $\tau(Paul)$ is user
 - 2.τ(Doom) is file
 - $3.Doom/xc \in dom(Peter)$
 - 4.Link(Peter, Paul) = TRUE
 - $5.\tau(Doom)/x \in f(\tau(Peter), \tau(Paul))$ because of 1 and 2

Therefore, Peter can give ticket *Doom/xc* to Paul

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SPM Example2



- Take-Grant Protection Model
 - \bigcirc TS = { subjects }, TO = { objects }
 - \bigcirc RC = {tc, gc}, RI = {rc, wc}
 - Note that all rights can be copied in T-G model
 - $\bigcirc link(\mathbf{p}, \mathbf{q}) = \mathbf{p}/t \in dom(\mathbf{q}) \lor \mathbf{q}/t \in dom(\mathbf{p})$
 - of(subject, subject) = { subject, object } x { tc, gc, rc, wc }
 - Note that any rights can be transferred in T-G model

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Demand



- A subject can demand a right from another entity
 - Operand function $d:TS \rightarrow 2^{TxR}$
 - OLet *a* and *b* be types
 - a/r.c ∈ d(b): every subject of type b can demand a ticket X/r.c for all X such that $\tau(X) = a$
 - A sophisticated construction eliminates the need for the demand operation – hence omitted

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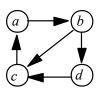
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Create Operation



- Need to handle
 - type of the created entity, &
 - tickets added by the creation
- Relation can•create(a, b) ⊂ TS x T
 - A subject of type a can create an entity of type b
- Rule of acyclic creates
 - Limits the membership in can•create(a, b)
 - If a subject of type a can create a subject of type b, then none of the descendants can create a subject of type a





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Create operation Distinct Types



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- create rule cr(a, b) specifies the
 - tickets introduced when a subject of type a creates an entity of type b
- **B** object: $cr(a, b) \subseteq \{ b/r: c \in RI \}$
 - Only inert rights can be created
 - \bigcirc A gets B/r:c iff b/r: $c \in cr(a, b)$
- B subject: cr(a, b) has two parts
 - \bigcirc $cr_P(a, b)$ added to **A**, $cr_C(a, b)$ added to **B**
 - \bigcirc **A** gets **B**/r.c if b/r.c in $cr_P(a, b)$
 - \bigcirc **B** gets **A**/r.c if a/r.c in $cr_{C}(a, b)$

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Non-Distinct Types



- cr(a, a): who gets what?
 - self/r:c are tickets for creator
 - a/r:c tickets for the created
- cr(a, a) = { a/r.c, self/r.c | r.c ∈ R}
- $cr(a, a) = cr_C(a, b)|cr_P(a, b)$ is attenuating if:
 - 1. $cr_C(a, b) \subseteq cr_P(a, b)$ and
 - 2. $a/r.c \in cr_P(a, b) \Rightarrow self/r.c \in cr_P(a, b)$
- A scheme is attenuating if,
 - O For all types a, $cc(a, a) \rightarrow cr(a, a)$ is attenuating

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Examples



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- Owner-based policy
 - O Users can create files: cc(user, file) holds
 - Oreator can give itself any inert rights: $cr(user, file) = \{file/r.c| r \in RI\}$
- Take-Grant model
 - O A subject can create a subject or an object
 - cc(subject, subject) and cc(subject, object) hold
 - Subject can give itself any rights over the vertices it creates but the subject does not give the created subject any rights (although grant can be used later)
 - $cr_{C}(a, b) = \Theta$; $cr_{P}(a, b) = \{sub/tc, sub/gc, sub/rc, sub/wc\}$ Hence,
 - cr(sub, sub) = {sub/tc, sub/gc, sub/rc, sub/wc} | ⊖
 - cr(sub, obj) = {obj/tc, obj/gc, obj/rc, obj/wc} | ⊖

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Safety Analysis in SPM



- Idea: derive maximal state where changes don't affect analysis
 - Indicates all the tickets that can be transferred from one subject to another
 - Indicates what the maximum rights of a subject is in a system
- Theorems:
 - A maximal state exists for every system
 - If parent gives child only rights parent has (conditions somewhat more complex), can easily derive maximal state
 - Safety: If the scheme is acyclic and attenuating, the safety question is decidable

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Typed Access Matrix Model



- Finite set T of types ($TS \subseteq T$ for subjects)
- Protection State: (S, O, τ, A)
 - \circ τ : $O \rightarrow T$ is a type function
 - Operations same as in HRU model except create adds type
- \bullet τ is child type iff command create creates subject/object of type τ
- If parent/child graph from all commands acyclic, then:
 - Safety is decidable
 - O Safety is NP-Hard
 - Safety is polynomial if all commands limited to three parameters

HRU vs. SPM



- SPM more abstract
 - Analyses focus on limits of model, not details of representation
- HRU allows revocation
 - OSPM has no equivalent to delete, destroy
- HRU allows multiparent creates, SPM does not
 - SPM cannot express multiparent creates easily, and not at all if the parents are of different types because can•create allows for only one type of creator
 - Suggests SPM is less expressive than HRU

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Comparing Models

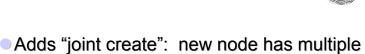


- Expressive Power
 - O HRU/Access Control Matrix subsumes Take-Grant
 - HRU subsumes Typed Access Control Matrix
 - SPM subsumes
 - Take-Grant
 - Multilevel security
 - Integrity models
- What about SPM and HRU?
 - SPM has no revocation (delete/destroy)
- HRU without delete/destroy (monotonic HRU)
 - O MTAM subsumes monotonic mono-operational HRU

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Extended Schematic Protection Mode



- OAllows more natural representation of sharing between mutually suspicious parties
 - Create joint node for sharing

parents

Monotonic ESPM and Monotonic HRU are equivalent

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