

# Reasoning and Decision Making

Comparisons to "Gold Standards"

not general models of reasoning, such as problem solving etc.

general finding: people don't meet gold standards

## Background issues:

### 1. Common sense reasoning:

Anderson: formal vs. human reasoning is architecture issue  
symbolic (formal) reasoning vs. neural models

But it is not an architecture issue

1. it is a question of fullness of knowledge representation
2. in limited domains expert systems are fine
3. neural systems have analogous problems or worse  
scaling is impossible w/o precision

### 2. Kinds of Logic:

propositional logic

p's and q's are variables that refer to entire (unanalyzed propositions)

first order predicate logic

similar to propositional notation seen earlier:

proposition consists of predicate (relation) + arguments

Fast(John)

$\square x \text{ Likes}(\text{John } x)$

$\square x \text{ Person}(x) \Rightarrow \text{Likes}(\text{John } x)$

rules in predicate logic

$\square x \text{ Bird}(x) \Rightarrow \text{Flies}(x)$

$\text{Bird}(\text{Tweety})$

$\text{Flies}(\text{Tweety})$                       ?how

Unify  $\text{Bird}(x)$  &  $\text{Bird}(\text{Tweety})$  by binding variable  $x$  to constant Tweety  
So...

$\text{Bird}(\text{Tweety}) \Rightarrow \text{Flies}(\text{Tweety})$

$\text{Bird}(\text{Tweety})$

$\text{Flies}(\text{Tweety})$

### 3. Some definitions

deductive reasoning

$a \rightarrow b$

$\frac{a}{b}$

"inductive reasoning" (two versions)

abductive reasoning

$a \rightarrow b$

$\frac{b}{a}$

inductive reasoning as concept formation

bird1 flies

bird2 flies

bird3 flies

.....

.....

all birds fly

### 4. Reasoning & Logic

psychological question-

relationship to logic

Boole 1854 "An investigation into the laws of thought"

(a deeper take on this)

# Deductive Reasoning and Problems with Conditional Reasoning

rules of inference:  
(permit valid deductions)

$p \rightarrow q$                   modus ponens  
 $p$  \_\_\_\_\_  
 $q$

$p \rightarrow q$                   modus tollens  
 $\sim q$  \_\_\_\_\_  
 $\sim p$

Rips & Marcus 1977

e.g.,  $p \rightarrow q$                   57% always  
 $\sim q$                                   39% sometimes  
\_\_\_\_\_                              4% never  
 $\sim p$

$p \rightarrow q$                   23% always  
 $q$                                       77% sometimes  
\_\_\_\_\_                              0% never  
 $p$

failure to apply modus tollens

Wason selection task:

each card:                  letter + number:  
rule:                                  vowel  $\rightarrow$  even number ?

example:                                  E K 4 7  
what to do to verify rule?

permission interpretation of conditional

Griggs & Cox 1982

if person is drinking beer  $\rightarrow$  person is over 19  
each card:                  age + drinking beer/coke

Cheng & Holyoak 1985

each card                                  transit/entering + vaccinations (?cholera)  
if entering  $\rightarrow$  cholera

better with rationale

Oaksford & Chater 1994

$p \rightarrow q$  means  $q$  is likely when  $p$  occurs  
and both are typically rare events

broken headlight  $\rightarrow$  broken taillight

broken headlight:	check taillight (correct)
not broken headlight:	don't check (correct)
broken taillight:	people check (incorrect logically but is confirming evidence)
not broken taillight:	people ignore (incorrect logically but not worth trouble)

# Reasoning about Quantifiers

## Categorical Syllogisms

2 premises -> conclusion  
each has categorical subject and predicate  
quantifiers: *all, no, some, some not*

e.g.,  
all A's are B('s)            some A's are B('s)  
all B's are C('s)        some B's are C('s)  
all A's are C('s)            some A's are C('s)

findings: people too willing to accept false syllogisms  
but there are patterns to people's responses

Explanations:

the atmosphere effect: Woodworth & Sells 1935

positive conclusion from positive positive premises  
negative conclusion from negative or mixed premises  
negative conclusion from mixed premises

no A's are B's  
all B's are C's  
no A's are C's

universal conclusion from universal premises  
particular conclusion from particular or mixed premises

all A's are B's  
some B's are C's  
some A's are C's

problems with hypothesis:

not functional (what or why)  
doesn't explain effect of validity  
doesn't explain effect of form

some A's are B's  
some B's are C's  
some A's are C's

some B's are A's  
some C's are B's  
some A's are C's

## Other Explanations:

- \* content effect (believability)

but people are accurate on valid syllogisms

- \* failure to accept logical task

- \* cultural and developmental differences

- \* failure to discriminate information in premises and information retrieved from memory

- \* forgetting premises

## Johnson-Laird: Mental Models

1. construct model of first premise

2. add info in second to model of first, taking into account various ways it can be done

3. frame a conclusion, if any, that holds in all the models

### Predictions of Theory-

1. difficulty depends on number of models

2. figural effects

fifo working memory

easier to state conclusion in same order

A-B B-C easiest

B-A C-B hold second, reprocess first

A-B C-B harder-

B-A B-C need to convert premise

## Reasoning about Probabilities

"gold standard" Bayes's Theorem:

$$\text{Prob}(H|E) = \frac{\text{Prob}(E|H)*\text{Prob}(H)}{\text{Prob}(E|H)*\text{Prob}(H) + \text{Prob}(E|\sim H)*\text{Prob}(\sim H)}$$

prior probability	$P(H)$	overlooked, often low
conditional probability	$P(E H)$	can be high and still
posterior probability	$P(H E)$	produce low posterior P

derivation of Bayes's Theorem

H: hypothesis is true,  $\sim H$ : hypothesis is false

E: evidence is true/present,  $\sim E$ : evidence is false/not present

H    $\sim H$

E   A   B

$\sim E$    C   D

$$\text{Prob}(E) = A + B$$

$$\text{Prob}(H|E) = A/A+B$$

so what are A, B, (and C, D) ?

does  $A = \text{Prob}(E)*\text{Prob}(H)$  ?? what would that assume?

$$A = \text{Prob}(H)*\text{Prob}(E|H) = \text{Prob}(E)*\text{Prob}(H|E)$$

$$B = \text{Prob}(\sim H)*\text{Prob}(E|\sim H) = \text{Prob}(E)*\text{Prob}(\sim H|E)$$

So:

$$\text{Prob}(H|E) = A/A+B$$

$$= \frac{\text{Prob}(E|H)*\text{Prob}(H)}{\text{Prob}(E|H)*\text{Prob}(H) + \text{Prob}(E|\sim H)*\text{Prob}(\sim H)}$$

## Explanations for discrepancies:

### Base Rate Neglect

Kahneman & Traversky 1973  
(30 engineers 70 lawyers)

### Conservatism

(too little attention to evidence)  
Edwards 1968  
choosing chips from bags

### Correspondance to BT with Experience

Gluck & Bower 1988  
patients w 4 symptoms  
\*what is wrong with this\*?

## Heuristics

Tversky & Kahneman, 1974  
availability  
representativeness

### gambler's fallacy

vs regression to the mean <=

## Decision Making

subjective utility

framing effects